

REŠITVE

1. a) $3a - 4 - 6a + 13 = -3a + 11$

b) $6x - (-x + 12) + 2 = 6x + x - 12 + 2 = 7x - 10$

c) $(3-x)(3+x) - 2(2x-4) = 9 - x^2 - 4x + 8 = -x^2 - 4x + 17$

d) $(x+1)(x-2)(x+2) = (x+1)(x^2-4) = x^3 - 4x + x^2 - 4$

2. a) $(x+5)^2 = x^2 + 10x + 25$ b) $(2x-8)^2 = 4x^2 - 32x + 64$ c) $(6x + \frac{2}{3})^2 = 36x^2 + 8x + \frac{4}{9}$

3. a) $(2y + \frac{9}{4})^2 = \frac{4y^2}{1} + \frac{36y}{4} + 81$ b) $\frac{x^2}{4} - 9y^2 = (\frac{x}{2} + 3y)(\frac{x}{2} - 3y)$

4. $(6x-2)(6x+2) - (5-6x)^2 =$ $x = -4$
 $= 36x^2 - 4 - (25 - 60x + 36x^2) =$
 $= 36x^2 - 4 - 25 + 60x - 36x^2 =$
 $= 60x - 29 =$
 $= 60 \cdot (-4) - 29 =$
 $= -240 - 29 =$
 $= -269$

5. a) $42a - 49b = 7 \cdot (6a - 7b)$

b) $15a^3b - 25a^2b^2 + 5ab^3 = 5ab(3a^2 - 5ab + b^2)$

c) $x^2 - 121 = (x-11)(x+11)$

č) $y^2 - 10y + 25 = (y-5)^2$

6. a) $\frac{8ab^4}{24a^3b^5} = \frac{8ab^4 \cdot 1}{24a^3b^5 \cdot 3a^2b} = \frac{1}{3a^2b}$

b) $\frac{a^2-4}{5a-10} = \frac{(a-2)(a+2)}{5(a-2)} = \frac{a+2}{5}$

c) $\frac{5a+15b}{(a+3b)^2} = \frac{5(a+3b) \cdot 1}{(a+3b)(a+3b) \cdot 1} = \frac{5}{a+3b}$

7. $\frac{x-1}{3x+6}$; a) $3x+6=0$ Uloomek mima
 $3x = -6$ pomona la
 $x = -2$ $x = -2$

b) $\frac{x-1}{3x+6} \Rightarrow \frac{2-1}{3 \cdot 2 + 6} = \frac{1}{6+6} = \frac{1}{12}$

$$8. a) \frac{x}{5} = 8 \quad \mathbb{R} = \{40\}$$

$$c) x^2 - 64 = 0 \quad \mathbb{R} = \{8, -8\}$$

$$(x-8)(x+8) = 0$$

$$b) 3(x+1) = 3x+3 \quad \mathbb{R} = \mathbb{R}$$

$$d) (x-7)(x-3) = 0 \quad \mathbb{R} = \{7, 3\}$$

$$3x+3 = 3x+3$$

$$3x-3x = 3-3$$

$$0x = 0 \quad \text{id.}$$

$$9. A. x(x-1) = x^2 - x$$

$$B. 2x = x + 8$$

$$C. x = 2x$$

$$D. 7x = 7x + 3$$

$$x^2 - x = x^2 - x$$

$$2x - x = 8$$

$$x - 2x = 0$$

$$7x - 7x = 3$$

$$\cancel{x^2} - \cancel{x^2} - x + x = 0$$

$$x = 8$$

$$-x = 0$$

$$0x = 3$$

$$0x = 0 \quad \mathbb{R} = \mathbb{R}$$

$$\mathbb{R} = \{8\}$$

$$x = 0 \quad \mathbb{R} = \{0\}$$

$$\mathbb{R} = \{\}$$

Enačba A je identična, enačba D pa nerisljiva.

$$10. a) 17 - 5x = 33 - 13x$$

$$L: 17 - 5 \cdot x =$$

$$D: 33 - 13x =$$

$$-5x + 13x = -17 + 33$$

$$= 17 - 5 \cdot 2 =$$

$$= 33 - 13 \cdot 2 =$$

$$8x = 16 \quad | :8$$

$$= 17 - 10$$

$$= 33 - 26 =$$

$$x = \frac{16}{8}$$

$$= 7$$

$$= 7$$

$$x = 2$$

$$b) x = \frac{x}{5} + 12 \quad | \cdot 5$$

$$L: 15$$

$$D: \frac{x}{5} + 12 =$$

$$x \cdot 5 = \frac{x \cdot 5}{5 \cdot 1} + 12 \cdot 5$$

$$= \frac{15}{5} + 12 =$$

$$5x = x + 60$$

$$= 3 + 12 =$$

$$5x - x = 60$$

$$= 15$$

$$4x = 60 \quad | :4$$

$$x = \frac{60}{4}$$

$$x = 15$$

$$c) \frac{x}{4} - 2 = \frac{x}{3} \quad | \cdot 12$$

$$L: \frac{x}{4} - 2 =$$

$$D: \frac{x}{3} =$$

$$\frac{x \cdot 12}{4} - 2 \cdot 12 = \frac{x \cdot 12}{3}$$

$$= \frac{-24}{4} - 2 =$$

$$= \frac{-24}{3} =$$

$$3x - 24 = 4x$$

$$= -6 - 2 =$$

$$= -8$$

$$3x - 4x = 24$$

$$-x = 24$$

$$x = -24$$

$$d) 6(7-2x) = 3-(1+2x)$$

$$42-12x = 3-1-2x$$

$$-12x+2x = -42+3-1$$

$$-10x = -40 \quad | :(-10)$$

$$x = \frac{-40}{-10}$$

$$x = 4$$

$$L: 6(7-2x) =$$

$$= 6 \cdot (7-2 \cdot 4) =$$

$$= 6 \cdot (7-8) =$$

$$= 6 \cdot (-1) =$$

$$= -6$$

$$D: 3-(1+2x) =$$

$$= 3-(1+2 \cdot (-4)) =$$

$$= 3-(1+8)$$

$$= 3-9 =$$

$$= -6$$

$$11.a) (x+3)^2 - 1 = (x-4)(x+2)$$

$$x^2+6x+9-1 = x^2+2x-4x-8$$

$$\cancel{x^2}+6x-\cancel{x^2}-2x+4x = -9+1-8$$

$$8x = -16 \quad | :8$$

$$x = \frac{-16}{8}$$

$$x = -2$$

$$L: (x+3)^2 - 1 =$$

$$= (-2+3)^2 - 1 =$$

$$= 1^2 - 1 =$$

$$= 1-1 =$$

$$= 0$$

$$D: (x-4)(x+2) =$$

$$= (-2-4)(-2+2) =$$

$$= (-6) \cdot 0 =$$

$$= 0$$

$$b) \frac{x+2}{4} - \frac{x-1}{8} = 1 \quad | \cdot 8$$

$$\frac{(x+2) \cdot 8^2}{4} - \frac{(x-1) \cdot 8^1}{8} = 1 \cdot 8$$

$$2(x+2) - (x-1) = 8$$

$$2x+4 - x+1 = 8$$

$$2x-x = -4-1+8$$

$$x = 3$$

$$L: \frac{x+2}{4} - \frac{x-1}{8} =$$

$$= \frac{3+2}{4} - \frac{3-1}{8} =$$

$$= \frac{5}{4} - \frac{2}{8} =$$

$$= \frac{5}{4} - \frac{1}{4} =$$

$$= 1$$

$$D: 1$$

$$12.a) \frac{5x}{6x^3} \cdot \frac{18x}{45} = \frac{5x \cdot 18x \cdot 1 \cdot 3}{6x^3 \cdot 45 \cdot 9 \cdot 1 \cdot 3x^2} = \frac{1}{3x^2}$$

$$b) \frac{x+7}{3y} \cdot \frac{y^5}{3x+21} = \frac{(x+7) \cdot y^5 \cdot y^4}{3y \cdot 3 \cdot (x+7)} = \frac{y^4}{9}$$

$$c) \frac{1}{4a} + \frac{11}{6a} - \frac{1}{3a} = \frac{3}{12a} + \frac{22}{12a} - \frac{4}{12a} = \frac{21}{12a} = \frac{7}{4a}$$

$$d) \frac{2x}{x-1} : \frac{8xy}{x^2-1} = \frac{2x \cdot (x+1)(x+1)}{(x-1) \cdot 8xy \cdot 4} = \frac{x+1}{4y}$$

$$e) \frac{1}{a+2} + \frac{3}{a+3} = \frac{1 \cdot (a+3)}{(a+2)(a+3)} + \frac{3(a+2)}{(a+2)(a+3)} = \frac{a+3+3a+6}{(a+2)(a+3)} = \frac{4a+9}{(a+2)(a+3)}$$

$$f) \frac{x}{5} - \frac{2-x^2}{2x} = \frac{x \cdot 5x}{10x} - \frac{(2-x^2) \cdot 5}{10x} = \frac{5x^2 - (10-5x^2)}{10x} = \frac{5x^2-10+5x^2}{10x} =$$

$$= \frac{10x^2-10}{10x} = \frac{10(x-1)}{10x} = \frac{x-1}{x}$$

$$g) \frac{b+3}{b} + \frac{1-a}{a} = \frac{(b+3) \cdot a}{ab} + \frac{(1-a) \cdot b}{ab} = \frac{\cancel{ab} + 3a + b - \cancel{ab}}{ab} = \frac{3a+b}{ab}$$

$$h) \frac{4x}{x-1} : \frac{8xy}{x^2-1} = \frac{\cancel{4x} \cdot (x-1)(x+1)}{(x-1) \cdot 8xy \cdot 2} = \frac{x+1}{2y}$$

1. Skrči izraze!

a) $3a - 4 - 6a + 13 =$

b) $6x - (-x + 12) + 2 =$

c) $(3 - x)(3 + x) - 2(2x - 4) =$

d) $(x + 1)(x - 2)(x + 2) =$

2. Kvadriraj dvočlenika!

a) $(x + 5)^2 =$ b) $(2x - 8)^2 =$ c) $\left(6x + \frac{2}{3}\right)^2 =$

3. Dopolni.

a) $(2y + \underline{\quad})^2 = \underline{\quad} + \underline{\quad} + 81$

b) $\frac{x^2}{4} - \underline{\quad} = (\underline{\quad} + 3y)(\underline{\quad} - 3y)$

4. Skrči izraz in izračunaj vrednost, če je $x = -4$.

$(6x - 2)(6x + 2) - (5 - 6x)^2 =$

5. Zapiši kot produkt (razstavi ali izpostavi)!

a) $42a - 49b =$

b) $15a^3b - 25a^2b^2 + 5ab =$

c) $x^2 - 121 =$

č) $y^2 - 10y + 25 =$

6. Okrajšaj ulomke:

a) $\frac{8ab^4}{24a^3b^5} =$ b) $\frac{a^2 - 4}{5a - 10} =$ c) $\frac{5a + 15b}{(a + 3b)^2}$

7. Za ulomek $\frac{x-1}{3x+6}$ določi,

a) za kateri x ulomek nima pomena: _____

b) Za $x = 2$ izračunaj vrednost danega ulomka. _____

8. Na črto zapiši množico rešitev danih enačb:

a) $\frac{x}{5} = 8$ _____

c) $x^2 - 64 = 0$ _____

b) $3(x + 1) = 3x + 3$ _____

d) $(x - 7)(x - 3) = 0$ _____

9. Dane so enačbe:

A. $x(x - 1) = x^2 - x$

B. $2x = x + 8$

C. $x = 2x$

D. $7x = 7x + 3$

DOPOLNI:

Enačba _____ je identična, enačba _____ pa nerešljiva.

10. Reši enačbe in naredi preizkus!

a) $17 - 5x = 33 - 13x$

b) $x = \frac{x}{5} + 12$

c) $\frac{x}{4} - 2 = \frac{x}{3}$

d) $6(7 - 2x) = 3 - (1 + 2x)$

11. Reši enačbi: (preizkus ni obvezen!)

a) $(x + 3)^2 - 1 = (x - 4)(x + 2)$

b) $\frac{x+2}{4} - \frac{x-1}{8} = 1$

12. Izračunaj, rezultati morajo biti okrajšani !

a) $\frac{5x}{6x^3} \cdot \frac{18x}{45} =$

b) $\frac{x+7}{3y} \cdot \frac{y^5}{3x+21} =$

c) $\frac{1}{4a} + \frac{11}{6a} - \frac{1}{3a} =$

d) $\frac{2x}{x-1} : \frac{8xy}{x^2-1} =$

e) $\frac{1}{a+2} + \frac{3}{a+3} =$

f) $\frac{x}{5} - \frac{2-x^2}{2x} =$

g) $\frac{b+3}{b} + \frac{1-a}{a} =$

d) $\frac{4x}{x-1} : \frac{8xy}{x^2-1} =$